\*\*\* The next section of the notes describes how to use various statistical tests in SPSS. You may also find the web page Which Statistical Test? useful. www.som.soton.ac.uk/learn/resmethods/statisticalnotes/which\_test.htm

## 24 Comparing Means and Medians

Suppose you wish to compare the means heights of females and males in our study. If you want to use parametric statistical procedures, then your assumption is that the data you have sampled was taken from a Normal distribution.

You can check your assumption by producing a Histogram with a Normal curve superimposed (**Graphs | Chart Builder** -select Histogram from the

**Chooses from** panel and drag into the Chart preview area. An Elements properties dialogue will be displayed.

Drag *Height (m)* from the variable list to the X-axis in the Chart preview window. Tick the *Display normal curve* box in the *Elements Properties* dialogue and click **Apply**.



Before carrying out any statistical

calculations, you should plot the data so that you can visually compare the data for the groups for any differences.

One approach could be to plot separate histograms for the groups (female and male). A better way to view the data is with a Box and



In the diagram opposite the Medians, represented by solid horizontal band, will be similar to the mean values for Normally distributed data. In this chart the medians are different and the boxes representing 50% of the data for each group and do not



overlap. So you can hypothesise from this that the mean heights of females and males are different.

#### Two Independent Samples: t-test

To test whether the observed difference between the mean heights of the female and male subjects in our study could have arisen by chance, select:

## Analyze | Compare Means | Independent-Samples T Test

An Independent-Samples T Test dialogue box is opened.

Click on *Height (m) height* and the upper to add this variable to the *Test Variable(s)* list.

Click on *gender*, the variable that defines the two categories and on the lower  $\bigcirc$  on to add it as the Grouping Variable.

Gender is displayed as *gender(? ?)* in the *Grouping Variable* box.

Click on the Define Groups button.

The Define Groups dialogue box allows the values that specify the two groups to be entered. Enter  $\underline{1}$  in the Group 1 box, press  $\langle tab \rangle$ 

Enter  $\underline{2}$  in the Group 2 box.

Click on Continue.

The Grouping Variable box of the Independent-Samples T Test will display *gender* (1 2).

The **Options** button in the Independent-Samples T Test dialogue box displays an *Options* dialogue box that allows the value for confidence intervals to be altered (default = 95%), value labels to be suppressed on the output and controls how missing values should be treated (List or Pairwise). These do not need to be altered. **Paste** and **Run** the command.

Output from SPSS t-test is shown below. Two tables are produced, one for Group Statistics and the other for the Independent Samples Test.

Group Statistics								
	Gender	N	Mean	Std. Deviation	Std. Error Mean			
Height (m)	Female	93	1.6261	.08751	.00907			
	Male	51	1.7675	.08035	.01125			

	independent Samples Test									
Levene's Test for Equality of Variances			t-test for Equality of Means							
									95% Confidenc Differ	e interval of the ence
		F	Sig.	t	df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	Lower	Upper
Height (m)	Equal variances assumed	.069	.793	-9.541	142	.000	1 41 39	.01482	17069	11210
	Equal variances not assumed			-9.782	110.735	.000	1 41 39	.01445	17004	11275

la deservate et Conseile e Torre

	Test Variable(s):	Ontions
<ul> <li>✓ Weight (kg) [ ▲</li> <li>▲ Long standing</li> </ul>	🔗 Height (m) [height]	Bootstrap
🗞 Registered di		
🚴 Reason 1 for		
Reason 2 for		
🗞 Reason 3 for		
Age (years) [A	Grouping Variable:	
🗞 Number of rea 🛛 🗾	Crouping variable.	
💰 senior	gender(77)	
💰 Age Categorie 🚽	Define Groups	
OK Paste	Reset Cancel Hel	D

ta Define Groups
<u>Use specified values</u>
Group <u>1</u> : 1
Group <u>2</u> : 2
© <u>C</u> ut point:
Continue Cancel Help

Before viewing the test statistics you should have decided if the variances (standard deviations squared) of the two groups are similar (equal) or not.

If the variances are similar, the top row of the table (Equal variances assumed) is used. If the variance are not similar the bottom row (Equal variances not assumed) is used. The important columns are the Mean Difference (-.14139) and the 95% Confidence Interval of the Difference (-.17069 to -.11210) together with the Sig (2-tailed) column which displays the P value (.000).

Note the negative values for the Difference and the Confidence Intervals of the difference occur because the female group, which is lighter, is the first group. If the male group had been the first group the values would have been positive.

## Comparing Two Medians: Mann-Whitney test

The Independent-Samples T Test used above assumes that the data are from populations that have a 'normal distribution', or that the sample sizes are large enough so that the distribution of the sample means is 'normal'. When the assumption of normality cannot be used, alternative techniques must be employed. These techniques are known as 'distribution-free' or 'non-parametric' statistics. They rely on the order or rank of the data rather than its distribution, 1 is smaller than 2; 4 is larger than 3. The fact that their differences are the same magnitude (2-1=1 and 4-3=1) is not a consideration.

In our data set you can consider that Age is not from a normal distribution because no case is under 17 years old (the subjects were sampled from a voting list). The distribution is truncated to the left.

Suppose you ask, is there a difference in the Ages of the females and males in this study?

The Box and Whisker plot compares the female and male data. This shows that the medians are very similar and there is complete overlap of the distributions.

Note: From this figure you might conclude that there is no point in testing for a difference because the median are similar. However we will demonstrate use of the procedure.



You can test for a difference between the ages of females and males by using the nonparametric equivalent of the T Test, the Mann-Whitney test. Select:

## Analyze | Nonparametric Tests| Legacy Dialogs | 2 Independent Samples

Highlight *Age of Respondent* and click the upper 🔛 button to add it to the Test Variable list.

Select *Gender* as the grouping variable. **Define Groups** as  $\underline{1}$  and  $\underline{2}$ .

Paste and Run the command.

Test Statist	csª	Date of Birth [d     Marital Status [
	Age (years)	Height (feet) [fe
Mann-Whitney U	2008.000	Weight (kg) [we
Wilcoxon W	3386.000	& Long standing i
z	-1.782	Test Type
Asymp. Sig. (2-tailed)	.075	Mann-Whitney U
a. Grouping Variable: Gender		Moses extreme reactions Wald-Wolfowitz runs
		OK Paste Reset Cancel Help

Two-Independent-Samples Tests

×

Tests statistics given by the non-parametric Two-Independent Samples Test shown above, provide very little useful information. The item of interest in this table is the *Asymp. Sig (2-tailed)*, or P value (.075). This indicates that there is no significant difference between the ages of females and males which could have been predicted by looking at the box plot.

Note: The output from all of the Non-parametric procedures in SPSS is poor. Typically, the only useful statistics the Asymp. Sig (2-tailed). You must use other SPSS procedures to obtain the medians of each group (e.g. Explore); confidence intervals are not calculated but can be obtained using the Confidence Interval Analysis Program, CIA.

### Paired samples t-test

*Note* The following is for illustration only. The data set you are using does not include any paired data.

A paired test is used when the data are matched or paired in some way. Often the subjects are used as their own control For example measuring something 'before' and 'after' an event. The paired t-test calculates the difference between paired data items and tests whether the average difference between paired measurements is different from zero.





Note: The paired Sample t-test can be used to test the difference between two variables where the original data are not from a Normal distribution if the distribution of the differences between the two readings approximate to a Normal distribution.

### The SPSS procedure would be: Analyze | Compare Means | Paired Samples T Test

The data for this procedure must be entered as two variables. These are selected by scrolling the list of variables and **clicking** on a variable and then clicking on to add it to the *Paired Variables* panel. If you select an incorrect variable, **clicking** on it in the Paired Variables panel (it will be highlighted in blue) and click to remove it.



The order of the variables (Weight 1 - Weight 2 or Weight 2 - Weight 1) can be set by clicking the button.

Output for the Paired Samples procedure is shown below. The mean difference of -1.3257 before minus after values ) suggests that our subjects lost weight! However, this difference is not significant (p = 0.108) and the change is due to random chance. You can tell this because the 95% confidence interval (-2.9940 to .2927) includes zero and also because the Sig (2-tailed) is 0.108.

				Fairea Sample:	5 1630				
		Paired Differences							
				95% Confidence Interval of the Difference					
		Mean	Std. Deviation	Std. Error Mean	Lower	Upper	t	df	Sig. (2-tailed)
Pair 1	Weight (kg) - Weight after 3 months	-1.3257	9.8594	.8188	-2.9440	.2927	-1.619	144	.108

### Non parametric Paired Samples: Wilcoxon

The nonparametric equivalent of the paired t-test is the Wilcoxon signed-rank test. This considers whether the difference is above or below zero. The procedure would be: Analyze | Nonparametric Tests | Legacy Dialogs | 2 Related samples Variables are selected in the same way as for the paired samples t-test procedure.

	Test Pairs	).			Exact
Case ID [id] Case ID [id] Case of Interview [doi] Case of Birth [dob] Case of Birth [	Pair 1 2 Test Typ ✓ Wicc: Sign McNei Margir	Variable1	Variable2	*	Options.

The only useful information displayed is the Asymp. Sig (2tailed) (P value), .108.



The calculation is Variable 2 – Variable 1 which the reverse of the paired t-test!

## 25 Comparing Proportions 2x2 tables

We are often interested in examining the relationship between two categorical variables. This may be achieved by cross-tabulating them in a contingency table. A useful convention (when appropriate) is for the rows of the table to correspond to the exposure values and the columns to the outcomes. You might ask whether gender is associated with registered disability, so gender is the "exposure" and regdisab (registered disabled) is the "outcome".

To create the table in SPSS select: Analyze | Descriptive Statistics | Crosstabs

Use Gender as the Row variable Crosstabs × Row(s): Exact. Registered Disabled [regdisab] as Case ID [id] 🖧 Gender [gender] \* Statistics. A Date of Interview [doi] the Column variable. Cells. A Date of Birth [dob] Column(s): Aarital Status [mstatus] Format. Registered disabled [reg. Height (feet) [feet] + Bootstrap.. Height (in) [inches] Weight (kg) [weight] Layer 1 of 1 long standing illness/d... Next 🖧 Reason 1 for no exerci.. Reason 2 for no exerci.. 🙈 Reason 3 for no exerci. -Age of Respondent [age] Display layer variables in table layers Display clustered bar charts Suppress tables OK Paste Reset Cancel Help

and

To improve the presentation and allow more detailed examination of the association by including marginal totals and percentages, click the **Cells** button and check the *Row Percentages*.

#### Click Continue

Click **Paste** and Run the command.

Counts Qbserved Expected Hide small counts Less than 5	Z-test Compare column proportions Adjust p-values (Bonferroni method)
Percentages          Row         Column         Total	Residuals <u>U</u> nstandardized <u>S</u> tandardized <u>A</u> djusted standardized
Noninteger Weights © Round cell counts © Truncate cell count © No adjustments	<ul> <li>◎ Round case weights</li> <li>s ◎ Truncate case weights</li> </ul>

Gender \* Registered disabled Crosstabulation

Count

Count

Count

% within Gender

% within Gender

% within Gender

Gender Female

Total

Male

Registered disabled

3

0

3

.0%

97%

No

16

12

28

84.2%

100.0%

90.3%

Total

100.0%

100.0%

100.0%

19

12

31

Yes

15.8%

The output is shows that there are 15.8% of females who are registered disabled and 0% of males.

A word of caution the number of Registered Disabled is very small so care must be taken with any statistical testing.

### Chi-squared test for a 2x2 table

Suppose you wish to assess the strength of the association between gender and registered disability. Use the Recall

dialog button is to recall the Crosstab procedure. Click the **Statistics** button.

Check the *Chi-square* box. Click **Continue Paste** and Run

× the Crosstabs: Statistics Chi-square Correlations Nominal Ordinal-Contingency coefficient 🔲 Gamma Phi and Cramer's V Somers' d 🗏 Lambda Kendall's tau-b Uncertainty coefficient Kendall's tau-c Nominal by Interval 🗏 Kappa 🔳 Eta Risk McNemar Cochran's and Mantel-Haenszel statistics Test common odds ratio equals: 1 Continue Cancel Help

The viewer will display as output:

Chi-Square Tests									
	Value	df	Asymp. Sig. (2-sided)	Exact Sig. (2- sided)	Exact Sig. (1- sided)				
Pearson Chi-Square	2.098 <sup>a</sup>	1	.148						
Continuity Correction <sup>b</sup>	.690	1	.410						
Likelihood Ratio	3.138	1	.076						
Fisher's Exact Test				.265	.216				
N of Valid Cases	31								

a. 2 cells (50.0%) have expected count less than 5. The minimum expected count is 1.16. b. Computed only for a 2x2 table

#### Interpreting the output

In this example you have small numbers, SPSS warns you in footnote b of the table above. Therefore the Pearson chi-square statistic which is the  $\chi^2$  test statistic is not appropriate in

this circumstance; Fishers Exact test should be used here (see below). If you had sufficient data you would use the (Asymp. Sig. 2-sided) = 0.148 which is the P-value and observe that is not significant.

### Yates' continuity correction

Some statisticians argue that the chi-squared test for a  $2x^2$  table can be improved by using a continuity correction, (Yates' continuity correction). In the output above the *P*-value is increased to .410.

#### Fisher's exact test

In this example an Exact test should be used to compare two proportions when the numbers in the 2x2 table are very small, leading to an expected value (in any cell) of less than 5. SPSS will report if any cells have expected values of less than 5 in which case the Fisher's exact test *P*-value should be reported. So you should report P=0.265.

#### Other statistics from Crosstabs

#### Paired Data (McNemar's test)

This is used when you have paired data for before and after studies, for example the presence of a condition (e.g. skin rash) is observed in subjects before and after an intervention. The  $\chi^2$  test is not appropriate because the data are not independent.

An example of this is: Seventy seven patients with diabetic nephropathy had one eye chosen at random to be treated while the other eye remained untreated. After five years follow-up the response variable (blind or not) was recorded for both eyes.

#### The kappa (κ) statistic

This allows you to assess the extent of the *reproducibility* of a measurement (also known as *reliability*), including:

- Agreement between different observers (inter-rater agreement) using the same measurement technique.
- Agreement between replicate measurements taken at different points in time.

## 26 Help with Statistical Procedures

To find out more about SPSS statistical procedures, Click the **Help** button in the procedure dialogue window, for example Crosstabs). A short description of the procedure is provided with an example and the statistics than can be calculated.



# 27 Further Reading

For a greater understanding of the issues and assumptions made when comparing means or medians you are advised to explore the following texts.

Practical Statistics for Medical Research, DG Altman, Chapman and Hall 1991. Chapter 9

*An Introduction to Medical Statistics*, 3<sup>rd</sup> Ed, M Bland, Oxford Medical Publications 2000. Chapters 10 and 12

*Medical Statistics: A textbook for the Health Sciences.* 4<sup>th</sup> Ed, MJ Campbell, D Machin & SJ Walters, Wiley 2007. Chapter 8

*Essential Medical Statistics*, 2<sup>nd</sup> *Ed* BR Kirkwood & JAC Sterne, Blackwell Science 2003. Chapters 7,9 & 30.

Medical Statistics at a Glance 3rd Ed, A Petrie & C Sabin, Wiley-Blackwell, 2009.